1 Practice Problems for Midterm Exam 2

Problem 1

A girl throws a water filled balloon of mass 0.1 kg at an angle 45° above the horizon. The highest point in the trajectory is reached after 0.86 seconds.

(a) What is the vertical component of the initial velocity? (5pts)
(b) What is the initial speed of the balloon? (5pts)
(c) The horizontal component of the balloon’s velocity is directed towards a car that is approaching the girl at a constant speed of 8 m/s. If the balloon is to hit the car at the same height at which it leaves her hand, what is the maximum distance the car can be from the girl when the balloon is thrown? Ignore air resistance, and I highly recommend not to try this at home. (10pts)
(d) How much work did the girl do launching the balloon? (5pts)
Problem 2

A bullet of mass $m_1 = 10$ g is fired with velocity $\vec{v}_1 = 300 \frac{m}{s}$ toward a stationary block of wood of mass $M_2 = 3$ kg, and is very rapidly brought to rest inside the block. The block is initially hanging from the ceiling by virtue of two massless strings as shown.

(a) What is the speed of the bullet and block just after the bullet is stopped (but before the combined mass has time to move an appreciable distance)?

(b) How high do the bullet and block rise relative to their initial height?

Problem 3

Wayne Gretzky is skating at 13.0 m/s towards a defender in the final national league game. The defender is skating at 5.0 m/s towards Gretzky. Gretzky’s weight is 756N and that of the defender is 900N. Immediately after the collision Gretzky keeps moving in his original direction at 1.5 m/s. You can ignore external horizontal forces applied by the ice to the skaters during the collision.

(a) What is the velocity of the defender immediately after the collision?

(b) Calculate the change in the combined kinetic energy of the two players?
Problem 4

The mass \( m_1 = 5 \text{kg} \) starts at rest on a frictionless surface 5 meters above the ground. It collides elastically with a mass \( m_2 = 10 \text{ kg} \) \( (15 \text{ kg}) \) once it reaches ground level.

a) What is the speed of \( m_2 \) after the collision?

b) What is the maximum height \( m_1 \) reaches after the collision?

Problem 5

A cart of mass \( m_1 = 0.200 \text{kg} \) moves on a horizontal air track with \( v_1 = 0.500 \hat{i} \text{ m/s} \). It collides elastically with a second cart \( (m_2 = 0.300 \text{ kg}) \) initially at rest.

(a) Compute the initial kinetic energy of the system.

(b) Find the final velocities of \( m_1 \) and \( m_2 \).

(c) If the collision occurs in 0.1 s, what is the average force exerted by car 1 on car 2?

**NOTE:** As shown in class (and the textbook) for elastic collisions in one dimension we can replace the kinetic energy formula with:

\[
\begin{align*}
  v_1 - v_2 &= -(v_1' - v_2')
\end{align*}
\]  

(1)
Problem 6

A rocket of mass \( M = 30.0 \text{ kg} \) is travelling with velocity \( \vec{V} = 1500 \text{ m/s} \) (horizontally) when it explodes into two chunks of mass \( m_1 = 20.0 \text{ kg} \) and \( m_2 = 10.0 \text{ kg} \). The mass \( m_1 \) is observed to be moving at an angle \( \theta_1 = 30.0^\circ \) above the horizontal with a speed \( |\vec{v}_1| = 1000 \text{ m/s} \) just after the explosion.

(a) Find the magnitude and direction of the velocity of \( m_2, |\vec{v}_2|, \) and \( \theta_2 \).

[HINT: You may need to know that \( \tan \theta = \frac{\sin \theta}{\cos \theta} \) and \( \sin^2 \theta + \cos^2 \theta = 1 \).]

(b) Do a calculation that allows you to determine whether this explosion was an elastic or inelastic process.

Problem 7

Two blocks of masses \( m = 1 \text{ kg} \) and \( M = 3 \text{ kg} \) are held at the distance \( d = 10 \text{ cm} \) against the force of a compressed spring between them. Then the blocks are released and are pushed apart by the spring. Assume that there is no friction. The spring is massless, has a force constant \( k = 200 \text{ N/m} \), and an unstressed length of \( l = 15 \text{ cm} \). Find

a) The total kinetic energy of blocks after “collision”.

b) Final velocities of blocks.
Problem 8

The angle $\theta$ through which a bicycle wheel turns is given by $\theta(t) = a + bt^2 - ct^3$ where $a$, $b$, and $c$ are positive constants such that for $t$ in seconds $\theta$ is in radians.

(a) Calculate the angular acceleration of the wheel as a function of time.

(b) At what time is the angular velocity of the wheel instantaneously not changing?

Problem 9

Three small blocks, each with mass $m$, are clamped at the ends and at the center of a massless rod of length $L$. (The rod is massless, do you think you need to include the moment of inertia of the rod?)

(a) Compute the moment of inertia of the system about an axis perpendicular to the rod and passing through a point $1/4$ of the length from one end.

(b) Compute the moment of inertia of the system about an axis perpendicular to the rod and passing through the center of the rod using the "parallel axis theorem" for moment of inertia.

(c) Check that your answer is correct by explicitly calculating the moment of inertia about the axis in (b)