

Formulas that might be memorized (but it is equally if not more important to understand the derivation well enough that you could derive these in a minute or two.)

$$k_F = (3\pi^2 n)^{1/3} \quad \text{where } n \text{ is the number density of "free" electrons in a metal}$$

$D(\epsilon_F) = 3n / 2\epsilon_F$ States per energy per volume (for both spins) at the Fermi level, in a free electron gas in 3d.

$$D(\epsilon) = D(\epsilon_F) (\epsilon / \epsilon_F)^{d/2-1} \quad \text{Free electrons in any number of dimensions}$$

$$\omega_p = (4\pi n e^2 / m)^{1/2} \quad \text{Free electrons}$$

$\epsilon = 1 + 4\pi i \sigma / \omega$ This follows from the Maxwell idea of $\partial P / \partial t$ as the current of the bound charges

$\epsilon = 1 - \omega_p^2 / \omega(\omega + i / \tau)$ Metals in free-electron approximation if ω_p is written as above. However, the formula is more generally applicable because ω_p can be generalized.

$\sigma = n e^2 \tau / m$ for currents carried by electronic quasiparticles as in a metal or a nicely doped semiconductor. The units are tricky. If cgs units are used, the unit of σ is s^{-1} , consistent with the equation $\epsilon = 1 + 4\pi i \sigma / \omega$. If you use SI (same as mksa) units, then σ has the correct dimensions of $C^2 s / kg m^3 = C^2 / J s m = A / V m = 1 / \Omega m$. To convert σ in SI to σ in cgs, you multiply by $1 / 4\pi \epsilon_0 = 9 \times 10^9 \text{ Jm} / C^2$. Perhaps I will give you σ and ask you to find τ .