

# Physics 301/571: Electromagnetic Theory I

**Read: Griffiths** chapter 2.4-2.5, 3.2

“G” refers to Griffiths’ book.

Problems with stars are not for credit and will NOT be graded.

## Homework 5

### Exercise 1

Eight particles of mass  $m$  and electric charge  $-q$  each are placed in corners of a cube and released. Find the velocity of each charge at infinity. The length of the edge of the cube is  $a$ .

### Exercise 2 (G 2.35)

A metal sphere of radius  $R$ , carrying charge  $q$ , is surrounded by a thick concentric metal shell (inner radius  $a$ , outer radius  $b$ ). The shell carries no net charge.

- Find the surface charge density  $\sigma$  at  $R$ , at  $a$ , and at  $b$ .
- Find the potential at the center, using infinity as the reference point.
- Now the outer surface is touched to a grounding wire, which lowers its potential to zero (same as infinity). How do your answers to (a) and (b) change?

### Exercise 3 (G 2.38)

A metal sphere of radius  $R$  carries a total charge  $Q$ . What is the force of repulsion between the “northern” and “southern” hemisphere?

### \*Exercise 4 (G 2.39)

Find the capacitance per unit length of two coaxial (very long) metal cylindrical tubes, of radii  $a$  and  $b$ .

### Exercise 5

What is the minimal work required to move a point charge  $q$  from the center of a thick concentric metal shell (inner radius  $a$ , outer radius  $b$ ) to infinity. Assume that there is a small hole in the shell.

### Exercise 6 (2d electron gas)

Two electrons are confined to a two-dimensional  $xy$  plane (can freely move along the plane, but have a fixed coordinate  $z = 0$ ). There is an infinite conducting plane (gate) parallel to the  $xy$  plane at the distance  $a$  from the latter ( $z = a$ ). Find the “effective” force between electrons at distances  $r \gg a$ . Take into account the “screening” by image charges.