

## Physics 501: Classical Mechanics

Read: LL 25-26, 31-36;

Problems with stars are not for credit and will NOT be graded.

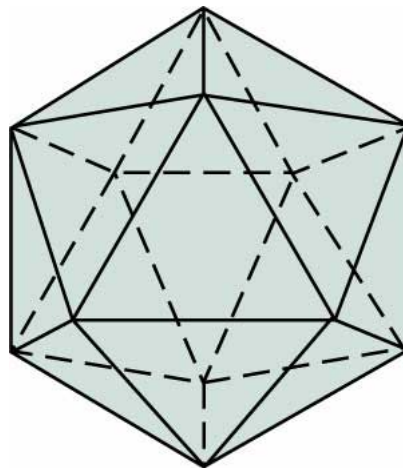
### Homework 6

#### Exercise 1

Estimate quality factors of a church bell and of a simple children's toy bell.

#### Exercise 2

Calculate the inertia tensor of a molecule consisting of 12 identical atoms of the mass  $m$  each forming an icosahedron (the radial size of the icosahedron is  $R$ ).



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Figure 1: To Exercise 2.

#### Exercise 3

A solid homogeneous cube occupies the region of space given in some reference frame by  $0 \leq x, y, z \leq a$ . Calculate the inertia tensor of the cube in this reference frame.

### Exercise 4

A solid homogeneous ball of the radius  $R$  has a spherical cavity of the radius  $r$  with the center at the distance  $a$  from the center of the ball. Choose a convenient reference frame and calculate the inertia tensor of this body.

### Exercise 5

A neutron star of the mass  $M = 3 \times 10^{30}$ kg and radius  $R = 10$ km rotates with the frequency  $f = 100$ Hz. The star (pulsar) has a magnetic moment and radiates electromagnetic energy with power  $P = 3.8 \times 10^{32}$ W. Find the rate with which it slows down its rotation. For example, you can find the relative change of the frequency of rotation for the period  $\Delta f/f$ .

### Exercise 6 (JS 8.3)

Calculate the rotation matrix  $R(\theta)$  that results from a rotation of  $\theta$  about the 3 axis followed by another of  $\theta$  about the 2 axis. Now calculate the result of applying them in the opposite order. Note the difference. Specialize to  $\theta = \pi/2$ . Find the axes and angles of the resulting  $\pi/2$  rotations.