

# Physics 540: Statistical Mechanics I

Read: LL 19,15,24

“LL 1” means section 1 from Landau and Lifshitz book

## Homework 3

### Exercise 1

The thermodynamic system consists of a hot brick of temperature  $T_1$  and specific heat  $C$  and of an iceberg at  $T_2 = 0^\circ\text{C}$ . What is the maximal work  $W$  that can be performed by bringing this system to the state of thermal equilibrium? Consider the effects due to the change of the total volume of the system as negligible.

### Exercise 2

In the presence of magnetic field  $H$  one defines magnetization of the body as  $\mathcal{M} = -\left(\frac{\partial E}{\partial H}\right)_{S,V}$ . Then one thinks about the energy as of function of three independent thermodynamic variables  $E = E(S, V, H)$  with  $dE = TdS - PdV - \mathcal{M}dH$ .

Assume that we know the complete equation of state  $P(T, V, H)$ , the temperature dependence of (constant volume, constant magnetic field) specific heat  $C_V(T, V_0, H_0)$  at some given  $V_0$  and  $H_0$  and temperature and magnetic field dependence of magnetization  $\mathcal{M}(T, V_0, H)$  at some given  $V_0$ .

- Show that there are 6 independent thermodynamic coefficients for such a system.
- Show that this data gives all 6 independent thermodynamic coefficients.
- Find the full dependence of  $C_V(T, V, H)$  and  $\mathcal{M}(T, V, H)$  from this data.