

Physics 302/572: Electromagnetic Theory II

Read: Griffiths 10.2-10.3

“G, PS” refer to Griffiths and Pollack & Stump books respectively. Problems with stars are not for credit and will NOT be graded.

Homework 7

Exercise 1 (G 10.11)

Suppose $\vec{J}(\vec{r})$ is constant in time. In this case it is easy to show that the charge density is a linear function of time $\rho(\vec{r}, t) = \rho(\vec{r}, 0) + \dot{\rho}(\vec{r}, 0)t$. Show that

$$\vec{E}(\vec{r}, t) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}', t)}{R^2} \hat{R} d\tau';$$

that is, Coulomb’s law holds, with the charge density evaluated at the *non-retarded* time.

Exercise 2 (G 10.18)

Suppose a point charge q is constrained to move along the x axis. Show that the fields at points on the axis to the *right* of the charge are given by

$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{1}{R^2} \left(\frac{c+v}{c-v} \right) \hat{x}, \quad \vec{B} = 0.$$

What are the fields on the axis to the *left* of the charge?

*Exercise 3 (G 10.19)

Using the formulas for electric and magnetic fields of a point charge moving with a constant velocity

- Calculate the electric field at a distance d from an infinite straight wire carrying a uniform line charge λ , moving at a constant speed v down the wire.
- Calculate the *magnetic field* of this wire.

Exercise 4 (G 10.24)

One particle, of charge q_1 , is held at rest at the origin. Another particle, of charge q_2 , approaches along the x axis, in hyperbolic motion:

$$x(t) = \sqrt{b^2 + (ct)^2};$$

it reaches the closest point, b , at time $t = 0$, and then returns out to infinity.

- a) What is the force F_2 on q_2 (due to q_1) at time t ?
- b) What total impulse ($I_2 = \int_{-\infty}^{+\infty} F_2 dt$) is delivered by q_2 to q_1 ?
- *c) What is the force F_1 on q_1 (due to q_2) at time t ?
- *d) What total impulse ($I_1 = \int_{-\infty}^{+\infty} F_1 dt$) is delivered by q_1 to q_2 ?

Answer: $I_2 = -I_1 = \frac{q_1 q_2}{4\epsilon_0 b c}$.

Exercise 5 (PS 15.21)

Calculate the Poynting vector and energy density of the electromagnetic field of a charged particle moving with constant velocity. Show that the field energy is carried along with the particle.