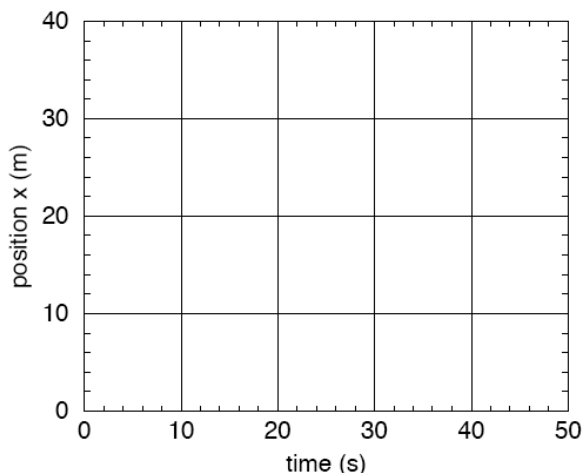
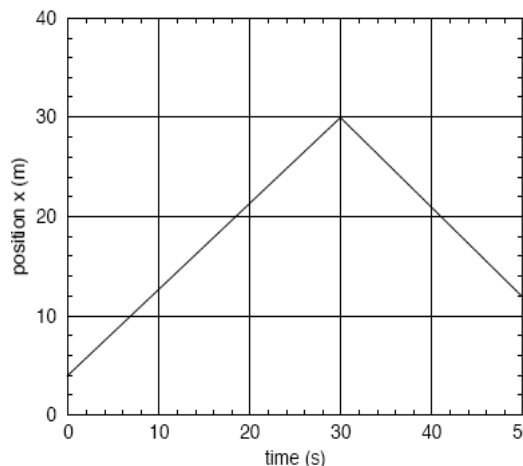


Cooperative Learning: work together, and submit one solution to each problem. A “solution” is not just a number. The reasoning needs to be indicated. The units of the number need to be specified. If the answer is a vector, the vector needs to be specified. Magnitude alone is not usually enough. **Write all 3 names on each page you submit.** No more than one page per problem.

1. Graphs; speed versus velocity.

In the graph to the right:

- What is the total distance travelled (the total length of the “path”)? $26\text{m} + 18\text{m} = 44\text{m}$
- What is the total displacement? $12\text{m} - 4\text{m} = 8\text{m}$
- What is the speed during the first 30s? 0.87 m/s
- What is the velocity during the last 20s? -0.90 m/s
- What is the average speed? $44\text{m}/50\text{s} = 0.88\text{ m/s}$
- What is the average velocity? $8\text{m}/50\text{s} = 0.16\text{ m/s}$



2. Graphs: accelerated motion.

A particle moves along the x axis. Its position as a function of time is given by $x=2.0t-t^2/30$, where t is in s (seconds) and x is in m (meters). **By derivatives, $v(t)=2.0-t/15$, and $a(t)=-1/15$.**

- Graph this motion (on the graph to the left).
- What is the velocity at time $t=0$? 2.0 m/s
- What is the velocity at time $t=50\text{s}$? -1.33 m/s
- What is the acceleration at time $t=0$? -0.067m/s^2
- What is the acceleration at time $t=50\text{s}$? **same**
- What is the average velocity from $t=0$ to 50s ? $16.7\text{m}/50\text{s} = 0.33\text{ m/s}$

3. Let y designate vertical position, with $y=0$ being the ground. A ball is launched upwards at time $t = 0$, with $v_y = 19.6\text{ m/s}$, starting from a height $y_0 = 2.0\text{ m}$.

- At what time is the ball at its maximum height? $t=(19.6\text{m/s})/(9.8\text{m/s}^2)=2.00\text{ s}$
- How high does the ball go? $v_{av} t=(9.8\text{m/s})(2.00\text{s})=19.6\text{ m}$
- What is the velocity when it returns to the original height y_0 going down? -19.6m/s
- What is the velocity of the ball when it is just about to hit the ground? $v^2 = v_0^2+2as$ where $a = -9.8\text{m/s}^2$ and $s=-2.0\text{m}$, so $v=-20.6\text{ m/s}$ (notice the negative root must be used.)
- At what time does the ball hit the ground? To go from -19.6m/s to -20.6 m/s takes $1.0/9.8 = 0.10\text{ s}$; The total time is $2 \times 2.00\text{s} + 0.10\text{ s} = 4.10\text{ s}$.
- What is the average velocity of the ball from time $t=0$ until it hits the ground? **Since acceleration is constant, $v_{av} = (v_0 + v_f)/2 = (19.6-20.6)/2 = -0.50\text{m/s}$. This is also the displacement -2.0m divided by the time $4.10\text{ s} = -0.49\text{ m/s}$ (expected round-off error!)**