

Cooperative Learning: work together**1. Vectors.**

In the graph to the right, using 2 significant figures:

- a. Specify vector \vec{B} in terms of components (B_x, B_y).

$$\vec{B} = (2.0, -1.0)$$

- b. Specify \vec{B} in terms of direction and magnitude.

$$|\vec{B}| = \sqrt{5.0} = 2.2, \text{ angle} = \tan^{-1}(-0.50) = -27^\circ.$$

- c. Draw the vector $\vec{A} - \vec{B} + \vec{C}$.

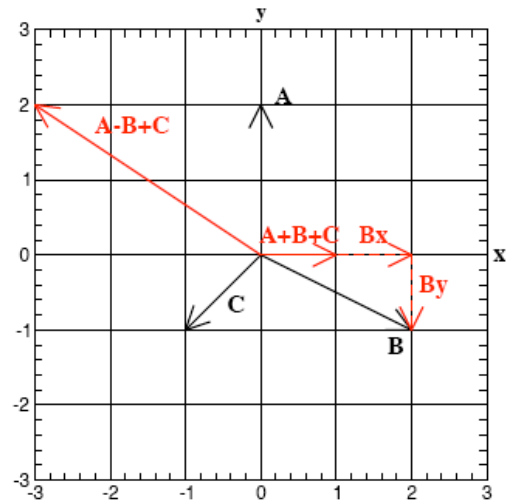
- d. Specify $\vec{A} - \vec{B} + \vec{C}$ in terms of components.

$$\vec{A} - \vec{B} + \vec{C} = (-3.0, 2.0)$$

- e. Specify $\vec{A} + \vec{B} + \vec{C}$ in terms of components.

$$\vec{A} + \vec{B} + \vec{C} = (1.0, 0.0)$$

- f. What is the angle from \vec{B} to \vec{C} (clockwise). $\tan^{-1}(2.0) + \tan^{-1}(1.0) = 63 + 45 = 108^\circ$.

**2. Projectile in 2d**

A projectile is shot from ground level, at an angle of 60.0° degrees above horizontal, and at a speed of 90.0 m/s . The ultimate aim is to find where it lands. Here is a logical way of breaking it into small easy steps.

- a. What is the vertical component of the initial velocity? $v_{y0} = v_0 \sin(60^\circ) = 77.9 \text{ m/s}$

- b. What is the horizontal component of the initial velocity? $v_{x0} = v_0 \cos(60^\circ) = 45.0 \text{ m/s}$

- c. How long will it take the projectile to reach the top of its trajectory? $t_t = v_{y0} / g = 7.95 \text{ s}$

- d. How far does it go horizontally in this time? $v_{x0} t_t = 358 \text{ m}$.

- e. Why are the time to land and the horizontal distance, twice the previous two answers?

$|v_y|$ depends only on height (y); positive going up, negative going down, symmetric.

- f. Graph the trajectory (as usual, vertical is y , horizontal is x .)

3. Another projectile in 2d

You need to throw a ball over a fence that is 20.0 m high and 30.0 m away. You launch the ball from an initial height of 2.0 m .

- a. What is the minimum v_y needed to make the ball go as high as the fence?

$$v_{y0} = \sqrt{(2g\Delta h)} = 18.8 \text{ m/s (using } \Delta h = 20.0 \text{ m} - 2.0 \text{ m)}.$$

- b. How much time does it take to reach this height? $(18.8 \text{ m/s}) / (9.8 \text{ m/s}^2) = 1.91 \text{ s}$.

- c. What is the correct v_x needed to make the ball clear the fence? $30.0 \text{ m} / 1.91 \text{ s} = 15.6 \text{ m/s}$

- d. What is the angle (above horizontal) at which you need to throw the ball?

$$\tan^{-1}(18.8 / 15.6) = 50.2^\circ$$

- e. What is the initial speed the ball needs to have? $\sqrt{((15.6)^2 + (18.8)^2)} = 24.4 \text{ m/s}$

- f. What is the average velocity of the ball from time $t=0$ until it hits the ground?

The x -component of the average velocity is just $v_{x0} = 15.6 \text{ m/s}$. The y component is the y distance (-2.0 m) divided by the time ($2 \times 1.91 \text{ s}$ plus an extra 0.1 s to fall an extra 2 m); $v_{\text{avg}} = (15.6, -0.52) \text{ m/s}$.