

Due Wednesday October 24 (note: midterm exam is Friday October 26)

1. Curie Law. The figure is from S. Arajis and R. V. Colvin, J. Appl. Phys. **33**, 2517 (1962).  $Gd^{3+}$  has a  $4f^7$  configuration, with approximately 7 Bohr magnetons of moment per ion. The data agree fairly well with the Curie Law. Derive the Curie Law.

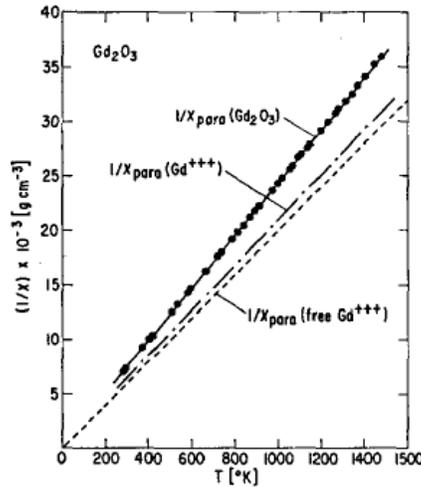


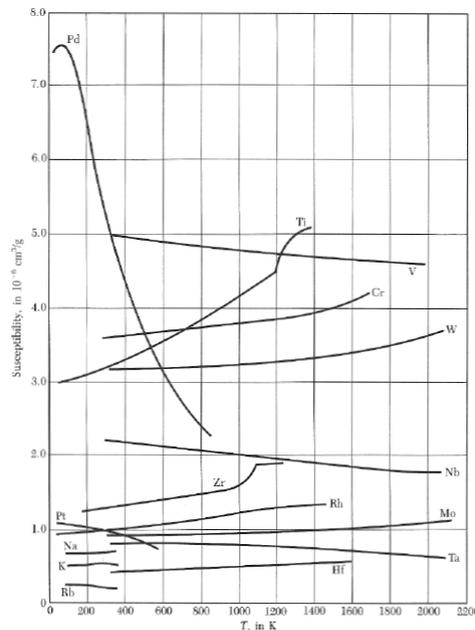
FIG. 1. Inverse magnetic susceptibility of  $Gd_2O_3$  as a function of temperature.

2. The Curie law should work only when spins on neighboring ions don't interact. Quantum mechanics allows a

strong exchange interaction which is apparently not important in  $Gd_2O_3$ . But there must always be a dipole-dipole classical interaction. As an estimate of the temperature below which the Curie law should fail, calculate the optimum attractive energy of (dipole-dipole) interaction of two Gd moments on nearest neighbor sites in  $Gd_2O_3$ . Estimate the spacing from the density  $\rho = 8.33 \text{ g/cm}^3$ .

3. In metals with weak exchange interactions between spins, the susceptibility (as explained by Pauli) is smaller than the Curie law by the small factor  $\sim k_B T/E_F$ . Derive the Pauli susceptibility. Assume an ordinary metal with a density of states  $D(E)$  which varies slowly with  $E$  on a scale of  $k_B T$ .

4. Aluminum metal has a Pauli susceptibility which is quite close to the free electron value. Suppose you put a gram of Al near a strong magnet, in a region with  $B = 1 \text{ T}$  and  $dB/dx = 100 \text{ T/m}$ . How large is the force (compared with  $mg$ , for example.)? You may use the free electron approximation.



**Note:** The figure to the right is from C. Kittel, *Introduction to Solid State Physics* (6<sup>th</sup> edition, Ch 14 – J.Wiley & Sons, 1986). It shows the susceptibility of various metals to rather high  $T$ , with some mild deviations from the  $T$ -independent Pauli form, except for Pd which deviates fairly strongly. It is not accidental that Pd also has the largest low  $T$  value.